A Quantified Study of Facial Asymmetry in 3D Faces *

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ABSTRACT

With the rapid development of 3D imaging technology, the wide usage of 3D surface information for research and applications is becoming a convenient reality. This study is focused on a quantified analysis of facial asymmetry of more than 100 3D human faces (individuals). We investigate whether facial asymmetry differs statistically significantly from a bilateral symmetry assumption, and the role of global and local facial asymmetry for gender discrimination.

1 Introduction

The recent advent of 3-dimensional imaging technology has spurred on several new research questions regarding the development of precise human detection and identification algorithms. Most of the object detection research done in 3D has thus far focused on non-human objects. Several 3D descriptors have been developed for classification of objects that make use of localized surface matching, e.g. [7], and global symmetrical attributes of a surface [8]. Little research has been done in the area of human face identification using 3D media. However, 3D imaging technology has advanced so rapidly that performing a quick 3D scan of every person who passes through an airport security gate may become routine in the near future. Some researchers have already shown certain success in 3D face comparison [6, 1].

One of the common characteristics of human faces is that they are approximately bilaterally symmetrical. Previous work has explored both human facial symmetry and asymmetry in different applications. Vedov and Poggio [17] suggest that object detection within the 2D framework can be greatly simplified by exploiting the known symmetries of an object in 3D. In [15], Seitz and Dyer assume Mona Lisa’s face is bilaterally symmetrical to achieve realistic 3D morphing. Zhao and Chellappa [18], and Shimshoni et al [16] have also taken advantage of facial symmetry in 3D reconstruction of human faces. On the other hand, facial asymmetry has long been reported [4, 2, 3]. Especially, expression lateralization is commonly accepted in the psychology literature, where some findings show facial expression is more intense on the left side. For human identification purposes, half faces have been tried, with some reported differences in recognition rates when left and right face images are used alone [13], while others [5] did not report any differences. More recently, Liu et al have demonstrated that quantified facial asymmetry contains discriminating information for human identification under expression variations, and for expression classification across individuals on 2D videos [12, 10]. They show statistically significant improvements can be achieved by combining facial asymmetry with classic human identification algorithms [12, 10].

The diverse applications and opposing assumptions on human facial bilateral symmetry and asymmetry are the primary motivations for this current investigation on 3D human faces. The objectives of this study are to

1. define a set of 3D facial asymmetry measurements that are readily computable directly from 3D digitized data sets;
2. find out whether the computed 3D facial asymmetry differs statistically significantly
   • from a facial bilateral symmetry assumption, and
   • between genders (male versus female)

2 3D Face Data

The database of human 3D face images that we use in this study is maintained by researchers in the department of Computer Science at the University of South Florida, and sponsored by the U.S. Department of Defense, Defense Advanced Research Projects

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Agency (DARPA). The database contains one digitized scan (image) for each of $N = 111$ subjects (74 male; 37 female). All subjects have a "neutral" facial expression.

2.1 Data Format

Each image file is stored in the database in the form of a triangle mesh, which consists of $x$, $y$, $z$ coordinate triples (observed locations of the surface of the face), and a list of triangles (plane segments) connecting these points. The triangle mesh representation is commonly used as a piecewise linear approximation to the true surface of an object in 3D space. The raw data consists of approximately 200,000 mesh points and 250,000 triangles per subject. The images have been normalized with respect to seven user-selected landmark locations on the face via an affine transformation of the original data [1], such that they are bilaterally located with respect to the YZ-plane.

Refer to Figure 1 for an example of a rendered image from the database, with $x$, $y$, $z$ coordinate axes superimposed on a 3D head. The $x$ axis represents left-to-right displacement, $y$ axis front-back, and $z$ axis up-down of the head.

![Figure 1: Example rendered image from database with $x$, $y$, $z$ coordinate axes superimposed.](image)

2.2 Data Preprocessing

To increase computational efficiency, we have employed a triangle decimation algorithm [14] to produce a subsample of the original mesh down to 5% of the original data volume.

Since the focus of our analysis in this work is the asymmetrical attributes of the human face, we consider a more conceptually intuitive coordinate system by transforming each 3D image from its Cartesian coordinate system indexed by $(x, y, z)$ to a cylindrical coordinate system $(\theta, r, z)$, i.e.

$$\theta = \tan^{-1} \left( \frac{x}{y} \right), \quad r = \sqrt{x^2 + y^2}, \quad z = z. \quad (1)$$

Note that the YZ-plane, where $\theta = 0$, bisects a 3D face.

For convenience of computation, we impose a 2D grid pattern on each 3D face which covers the whole face from chin to forehead in the vertical $z$ direction, and from outside of one eye outer corner to outside the other eye in the $\theta$ direction (Figure 2). We split the grid into 125 equally spaced intervals in both the $\theta$ and $z$ directions, yielding a total of $125 \times 125 = 15,625$ grid points. For each of these 15,625 grid points, we interpolate its $r$ value (distance from the $z$-axis) using trilinear interpolation on the original surface mesh. See Figures 1 and 2 for a 3D face of the same subject in its rendered and meshed forms, and Figure 2 (right) for its texture map with the cropped region superimposed.

If we use $F_i$ to denote the original mesh data and $f_i$ the re-parametrized $F_i$: each 3D face $F_i$ in the database is now mapped into $f_i$, a 125 by 125 grid matrix with

$$f_i = r(\theta, z) \quad (2)$$

where $\theta$ takes on a discrete set of values in the range $[-0.75, 0.75]$ radians with increment 0.012, and $z$ takes on a discrete set of values in $[-50, 75]$.

3 3D Face Analysis

In this section we define a pair of facial asymmetry measures for 3D faces. These definitions are general and not limited to frontal faces.

3.1 3D Facial Asymmetry Measures

Let $\gamma$ represent a plane in 3D space passing through the origin. In general, $\gamma(\theta, \phi)$ is a function of rotation about the $z$-axis ($\theta$) and rotation about the $y$-axis ($\phi$). We are currently keeping $\phi$ fixed at 0 and varying $\theta$ only. If we further restrict $\gamma$ to only take on $\theta$ values that coincide with our grid definition, then with respect to each position of the $\gamma$ plane when $\theta = \theta_{\gamma}$, each point $p_i$ on a 3D face mesh with coordinates
\( (\theta_1 + \theta_2, r_i, z_i) \) has a corresponding reflected (with respect to \( \gamma \)) point \( p'_i \) with \( (\theta_2, r_i, z_i) \), given that the point is within the boundary of the grid.

For a given face \( f \) and plane \( \gamma \), we introduce the following asymmetry measurements:

**Height Difference (HD):**

\[
HD_{f,\gamma}(\theta, z) = |r(\theta, z) - r'_\gamma(\theta, z)|
\]

where \( r'_\gamma \) is the \( r \) value of face \( f \) at \( (\theta_2, \theta, z) \), the reflected point of \((\theta, z)\) with respect to plane \( \gamma \). We refer to \( \gamma \) as the symmetry plane.

**Orientation Difference (OD):**

\[
OD_{f,\gamma}(\theta, z) = \cos(\beta_{\theta_1,\theta_2})(\theta, z)
\]

where \( \beta_{\theta_1,\theta_2}(\theta, z) \) is the angle between the normal vector of the face mesh at grid point \((\theta, z)\), and the normal vector of its corresponding reflected point with respect to \( \gamma \).

For each 3D face \( f \) and plane of symmetry \( \gamma \) pair, the \( HD(f) \) and \( OD(f) \) functions both yield feature vectors with dimensions as high as the number of grid points. We refer to these measurements as HD-Face and OD-Face. Given the symmetry of the \( HD \), \( OD \) definitions, the left or right hand of \( HD \)-face (OD-face) contains all of the facial asymmetry information in \( HD \)-face (OD-face). Figure 3 shows the original mesh, the \( HD \)-Face, and the \( OD \)-Face for six subjects from the database. The top three rows in the figure are females and the bottom three rows are males.

### 3.2 Global Facial Asymmetry

To obtain an overall measure of asymmetry for a particular subject with respect to a plane of symmetry, we can take the average of all the values over the grid of \( HD \)-Face or \( OD \)-Face. The resultant value will be \( \| f - f_i \| \) where \( f_i \) is the reflection of \( f \) through the plane of symmetry \( \gamma \). So, we define the following global metrics:

**Overall Height Difference (OHD):**

\[
OHD_{f,\gamma} = \frac{1}{T} \sum_{\theta, z} |r(\theta, z) - r'_\gamma(\theta, z)|
\]

**Overall Orientation Difference (OOD):**

\[
OOD_{f,\gamma} = \frac{1}{T} \sum_{\theta, z} \cos(\beta_{\theta_1,\theta_2})(\theta, z)
\]

where \( I \) is the total number of grid points that have a corresponding reflected point on the grid. For \( \theta_1 = 0 \) (symmetry plane that bisects the head through the midline of the face into a right and left hemisphere), each point on the grid has a corresponding reflected point that is also on the grid (so, \( \gamma = 715 \times 62 = 7750 \)). For values of \( \gamma \) other than 0, however, there will be fewer grid points with which to use in the computation of \( OHD \) and \( OOD \).

### 4 Analysis Results

We start with an analysis of global 3D facial asymmetry of the \( OHD \) and \( OOD \) measurements, followed by a local analysis. We are looking into the question of whether there are statistically significant differences between the measured facial asymmetry of all subjects and the human facial bilateral symmetry assumption. We then compare male and female facial asymmetry globally and locally.

#### 4.1 Global Asymmetry

For each subject in the database with a 3D face \( f_i \), we vary the symmetry plane such that \( \theta_1 \in [-0.36, 0.36] \) radians. Table 1 shows the means and standard errors of \( OHD \) and \( OOD \) for a range of values of \( \theta_1 \). The question is: Do the mean asymmetry values differ significantly from the bilateral symmetry assumption?

<table>
<thead>
<tr>
<th>( \theta_1 ) (radians)</th>
<th>Mean</th>
<th>SE</th>
<th>Mean</th>
<th>SE</th>
</tr>
</thead>
<tbody>
<tr>
<td>-0.363</td>
<td>12.33</td>
<td>2.28</td>
<td>0.73</td>
<td>0.07</td>
</tr>
<tr>
<td>-0.302</td>
<td>13.13</td>
<td>2.22</td>
<td>0.67</td>
<td>0.04</td>
</tr>
<tr>
<td>-0.242</td>
<td>11.69</td>
<td>2.09</td>
<td>0.64</td>
<td>0.04</td>
</tr>
<tr>
<td>-0.181</td>
<td>10.07</td>
<td>1.74</td>
<td>0.58</td>
<td>0.03</td>
</tr>
<tr>
<td>-0.121</td>
<td>8.12</td>
<td>1.25</td>
<td>0.54</td>
<td>0.04</td>
</tr>
<tr>
<td>-0.060</td>
<td>4.81</td>
<td>0.82</td>
<td>0.41</td>
<td>0.04</td>
</tr>
<tr>
<td>0.000</td>
<td>1.44</td>
<td>0.35</td>
<td>0.20</td>
<td>0.03</td>
</tr>
<tr>
<td>0.060</td>
<td>4.94</td>
<td>0.80</td>
<td>0.40</td>
<td>0.04</td>
</tr>
<tr>
<td>0.121</td>
<td>8.28</td>
<td>1.22</td>
<td>0.54</td>
<td>0.04</td>
</tr>
<tr>
<td>0.181</td>
<td>10.29</td>
<td>1.73</td>
<td>0.58</td>
<td>0.03</td>
</tr>
<tr>
<td>0.242</td>
<td>11.97</td>
<td>2.07</td>
<td>0.64</td>
<td>0.04</td>
</tr>
<tr>
<td>0.302</td>
<td>13.45</td>
<td>2.20</td>
<td>0.67</td>
<td>0.04</td>
</tr>
<tr>
<td>0.363</td>
<td>12.75</td>
<td>2.33</td>
<td>0.73</td>
<td>0.07</td>
</tr>
</tbody>
</table>

As expected, with the increase of \( \theta_1 \) the values of \( OHD \) and \( OOD \) increase. Figure 4 shows the \( OHD \) and \( OOD \) plots, respectively, for all subjects in the database. It is interesting to note that the \( OOD \) measurement has a nearly constant variance for different values of \( \gamma \), while the variance of \( OHD \) is fanning out.
<table>
<thead>
<tr>
<th>Subject</th>
<th>Original mesh</th>
<th>HD-Face</th>
<th>OD-Face</th>
</tr>
</thead>
<tbody>
<tr>
<td>001, Female</td>
<td><img src="image1" alt="Image" /></td>
<td><img src="image2" alt="Image" /></td>
<td><img src="image3" alt="Image" /></td>
</tr>
<tr>
<td>008, Female</td>
<td><img src="image4" alt="Image" /></td>
<td><img src="image5" alt="Image" /></td>
<td><img src="image6" alt="Image" /></td>
</tr>
<tr>
<td>053, Female</td>
<td><img src="image7" alt="Image" /></td>
<td><img src="image8" alt="Image" /></td>
<td><img src="image9" alt="Image" /></td>
</tr>
<tr>
<td>002, Male</td>
<td><img src="image10" alt="Image" /></td>
<td><img src="image11" alt="Image" /></td>
<td><img src="image12" alt="Image" /></td>
</tr>
<tr>
<td>023, Male</td>
<td><img src="image13" alt="Image" /></td>
<td><img src="image14" alt="Image" /></td>
<td><img src="image15" alt="Image" /></td>
</tr>
<tr>
<td>037, Male</td>
<td><img src="image16" alt="Image" /></td>
<td><img src="image17" alt="Image" /></td>
<td><img src="image18" alt="Image" /></td>
</tr>
</tbody>
</table>

Figure 3: Original mesh images, HD-Faces, and OD-Faces for six subjects in the database. Top three rows are female and bottom three rows are male.
as the symmetry plane moves away from the frontal view. Also note the single abberant profile in the OOD panel of Figure 4, who upon inspection of Figure 3, appears to have a beard that contributes a large amount of asymmetry in terms of the vectors normal to the mesh. We have removed this subject from subsequent analysis.

![OHD and OOD](image)

Figure 4: Profile plots of global asymmetry measures. Left panel: OHD, Right panel: OOD.

The vertical reference line in Figure 4 signifies the frontal view plane of symmetry, note both the means and the variances of the 3D facial asymmetry measures are non-zero. Figure 5 shows the facial asymmetry distribution histograms with density estimates overlayed on the graphs, when the symmetry plane is the YZ-plane (frontal view). The outlier in the OOD measurements is the same subject 023 as in Figure 4.

![Histograms of OHD and OOD](image)

Figure 5: Histograms of global facial asymmetry measures when the symmetry plane \( \theta_\gamma = 0 \) with density estimates overlayed.

To assess the statistical significance of the level of global asymmetry we have observed on the frontal faces \( (\theta_\gamma = 0) \), we compare the distribution of the observed values to a null distribution of symmetric frontal faces. A perfectly symmetric face would ideally yield a global asymmetry measurement of zero. Any source of error, however, will yield a strictly positive measurement. Instead of attempting to isolate the various sources of error (measurement error from scanning device, error due to normalization process, and error introduced by decimation algorithm), we assume that a random process acts directly on the \( r(\theta, z) \) values and the normal vectors. We further assume that the errors act independently (no error covariance structure). With these assumptions, we estimate the null distribution in the following manner (discussion in terms of OHD): \( OHD_{\text{NULL}} = \frac{1}{\sigma} \sum \epsilon(\theta, z) \) where \( \epsilon \) are independent and identically distributed (iid) Gaussian random variates with expected value 0 and standard deviation \( \sigma \). Under the null hypothesis we have \( r(\theta, z) = r(\theta, z) \), the expected value of the global asymmetry measurement is: \( E(OHD_{\text{NULL}}) = E \left( \frac{1}{\sigma} \sum \epsilon(\theta, z) \right) \). We estimated the expected value of the null distribution for different levels of \( \sigma \) using a Monte Carlo Integration simulation. To assess significance, we compare the observed distribution (Mean = 1.44, SE = 0.35) to these estimates using a standard t-test. See Table 2 below for results for the OHD measure. For gaussian noise with \( \sigma < 0.8 \), we observe statistically significant bilateral asymmetry. Refer to Figure 6 for a comparison of left face from the original mesh data and right face being a reflected version of the left with \( \sigma = 0.8 \) noise added.

Table 2: Significance tests of global asymmetry for varying levels of gaussian noise.

<table>
<thead>
<tr>
<th>( \sigma )</th>
<th>( E(OHD_{\text{NULL}}) )</th>
<th>( SD(OHD_{\text{NULL}}) )</th>
<th>( p )-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.113</td>
<td>0.0121</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>0.2</td>
<td>0.226</td>
<td>0.0230</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>0.3</td>
<td>0.342</td>
<td>0.0343</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>0.4</td>
<td>0.456</td>
<td>0.0477</td>
<td>0.002</td>
</tr>
<tr>
<td>0.5</td>
<td>0.558</td>
<td>0.0587</td>
<td>0.006</td>
</tr>
<tr>
<td>0.6</td>
<td>0.673</td>
<td>0.0720</td>
<td>0.014</td>
</tr>
<tr>
<td>0.7</td>
<td>0.787</td>
<td>0.0824</td>
<td>0.031</td>
</tr>
<tr>
<td>0.8</td>
<td>0.904</td>
<td>0.0972</td>
<td>0.003</td>
</tr>
<tr>
<td>0.9</td>
<td>1.017</td>
<td>0.1164</td>
<td>0.113</td>
</tr>
<tr>
<td>1.0</td>
<td>1.126</td>
<td>0.1226</td>
<td>0.185</td>
</tr>
</tbody>
</table>

Similar noise simulation procedure is applied on OOD measure. We observe statistically significant results when we apply gaussian random noise with \( \sigma \leq \frac{\pi}{2\sigma} \) radians. In other words, if we assume that the error (in terms of displacement away from the normal vector) is governed by a gaussian process with standard deviation no greater than \( \frac{\pi}{2\sigma} \approx 7 \) degrees, then
the 3D faces in this dataset show statistically significant bilateral asymmetry using OOD measurement.

Since the image data is obtained using a scanner from Cyberware Inc. with comparable accuracies of 0.25mm and 0.013° as reported in [9], the noise level for this dataset is expected to be well below \( \sigma = 0.8 \) in height and 7 degrees in orientations.

Figure 6: Left side is the meshed face obtained from the original data, right side is a reflection of the left face with added gaussian noise at \( \sigma = 0.8 \). Obvious unsatisfactory imaging quality is observed on the right face. Our results (Table 2) show statistically significant facial asymmetry on 3D face images can be observed up to this level of noise (exclusive).

4.2 Global Frontal Face Asymmetry by Gender

Previous results have reported a facial asymmetry difference between genders (e.g., [4]). In this section we focus our attention on the relationship between facial asymmetry and the gender differences. Once again, we restrict our attention to the global asymmetry measures obtained for the frontal face (plane of symmetry corresponding to \( \theta_i = 0 \)). Figure 7 presents box-plots portraying the distributions of the two global measures by gender.

A simple t-test comparing the mean asymmetry value between males and females is statistically insignificant for the OHD measure (p-value=0.88), yet is **highly statistically significant for the OOD measure** (p-value < 0.001).

4.3 Local Frontal Face Asymmetry

We now turn our focus to the localized asymmetry vectors HD-Face and OD-Face. For this discussion, we will again restrict our attention to the frontal face.

Figure 7: Box-plots for global asymmetry measures divided by gender.

See the left column in Figure 8 for the average HD-Face and OD-Face (averaged over all subjects except the bearded outlier). The darker regions in the images represent areas of higher asymmetry. The images in the right column of Figure 8 show the top 20% most asymmetrical regions measured by HD-Face and OD-Face.

![Box-plots for global asymmetry measures divided by gender.](image1)

Average Faces (HD) | Top 20% Regions
---|---
![Image](image2)

Average Faces (OD) | Top 20% Regions
---|---
![Image](image3)

Figure 8: Average frontal HD-Faces and OD-Faces (left column), and top 20% most asymmetrical regions (right column).

It is clear from these average faces that there are significant trends in the regions of asymmetry for both types of asymmetry measurements. For the HD-Face, the regions with the highest asymmetry are around the sides of the nose and in the lower portion of the cheek area. For the OD-Face, the regions are the eyes, nostrils, and mouth. The two measurements appear to
complement one another quite well in that they capture different information about the regions of asymmetry of the frontal face.

4.4 Local Frontal Face Asymmetry by Gender

We will now investigate the differences in the local asymmetry measures (HD-Face and OD-Face) between male and female 3D faces. In particular, we are seeking to locate discriminative subspaces of the asymmetry features (facial asymmetry measures belong to certain subregions of the face) where male versus female facial asymmetries differ the most.

Each feature in the full range of HD-Face and OD-Face vectors is not equally important for discriminating between male and female faces. We attempt to reduce the size of the feature space (dimensionality of HD-Face and OD-Face) through the means of a variance ratio. In general, for a feature $F$ with $C$ total classes, we define the variance ratio as follows:

$$\text{vr}(F) = \frac{\text{Var}(F)}{C \sum_{i=1}^{C} \frac{\text{Var}(F)}{\text{mean}_i(F) - \text{mean}(F)}}$$

where $\text{mean}_i(F)$ is the mean of feature $F$’s values in class $i$. This variance ratio is the ratio of the variance of the feature between classes to the variance of the feature within classes, with an added penalty for features which may have small intra-class variance but which have close inter-class mean values.

Refer to Figure 9 for a feature-by-feature representation of $\text{vr}(F)$ applied to the HD- and OD- Faces with male and female as two gender classes ($C = 2$). The darker regions in the plot signify features that have higher $\text{vr}(F)$ values, and thus higher gender discriminating power.

Comparing Figures 9 and 8, one can observe a resemblance between the regions on the face with the highest gender discriminating power and the regions of high asymmetry measures.

If we retain those facial asymmetry features with the highest 1% $\text{vr}(F)$ values, a feature subspace of nearly 100 dimensions is obtained. Using this subspace in a logistic regression setting with gender acting as the dichotomous outcome, we observe a highly statistically significant difference between genders ($p$-value < 0.001 in both cases). This result suggests that there is enough information in the localized asymmetry measures between male and female faces.

Next, we construct a linear classifier similar to [12]: (1) rank the features of a training set by their respective $\text{vr}(F)$ values from high to low; (2) apply forward feature selection using linear discriminant analysis (LDA) on the ranked features to select a discriminative feature subspace; (3) test the result using the test set in the selected feature subspace. Randomly divide the dataset half-half (same male versus female ratio) for training and testing, and repeat the above classification process 100 times. We obtain mean classification error rates of 8.84% using HD-Face and 3.78% using OD-Face with a one standard deviation of 3.15% ($HD$) and 2.30% ($OD$) respectively. The average subspace dimension is 40 features for HD-Face and 43 features for OD-Face in our experiments. These results validate the hypothesis that there is sufficient discriminative information in the localized asymmetry measurements for gender classification.

5 Discussion and Conclusion

While 3D imaging technology is still in its formative stages of development, many current research efforts are showing promising gains towards the ultimate goal of constructing a completely autonomous 3D human identification system. We have attempted in this paper to quantify the level of asymmetry possessed by the 3D human face. We have also addressed the issue of whether there exists significant facial asymmetry in frontal faces and differences in asymmetry between males and females.

Two types of 3D facial asymmetry measures are
defined in this paper: height difference faces (HD-face) and orientation difference face (OD-face). From the statistical analysis, OD-face as a global measure presents itself as a more compact representation for facial asymmetry (Figure 4). Thus it is a good candidate for asymmetry-based pose estimation. OD-face also shows more significant departure from the bilateral symmetry assumption and better discriminating power between genders. On the other hand, HD face requires less computation cost and is less sensitive to outliers.

Our result on 3D human faces of more than 100 subjects shows that human facial asymmetry is statistically significant given a reasonable range of sensor noise, therefore facial asymmetry should not be ignored without a justification. If properly utilized, it is foreseeable that facial asymmetry may provide non-trivial contributions to human face analysis. One such example has been demonstrated for human identification under expression variations [12].

Our result on 3D facial asymmetry divided by gender supports early research in psychology that the male face possesses a larger amount of asymmetry than does the female face, and is in agreement with our preliminary study of facial asymmetry measurements computed from 2D expression videos [11]. We show that a statistically significant difference arises between male and female faces in terms of the OOD measurement, but not so with respect to the OHD measure. By analyzing 3D facial asymmetry locally, we are able to identify which part of the face that is most asymmetrical, and which part of the 3D face that is most discriminative in gender classification (Figure 9). This latter finding of regions around the nose bridge echoes the discriminative asymmetry measures found from expression videos for human identification [12]. The feature discriminative measure AVR is capable to rule out those features that have a large within class variance and small mean difference between classes, therefore mitigating the possibility for asymmetry features with large measurement noise to be chosen. We also show that (1) a statistically significant difference exists for both facial asymmetry measurements HD and OD between males and females; (2) by looking at a discriminative subspace of facial asymmetry features, we can achieve 91.16% and 96.22% gender classification rates, using LDA on HD and OD respectively.

References


